



# Rho meson effect in hadron-quark phase transition

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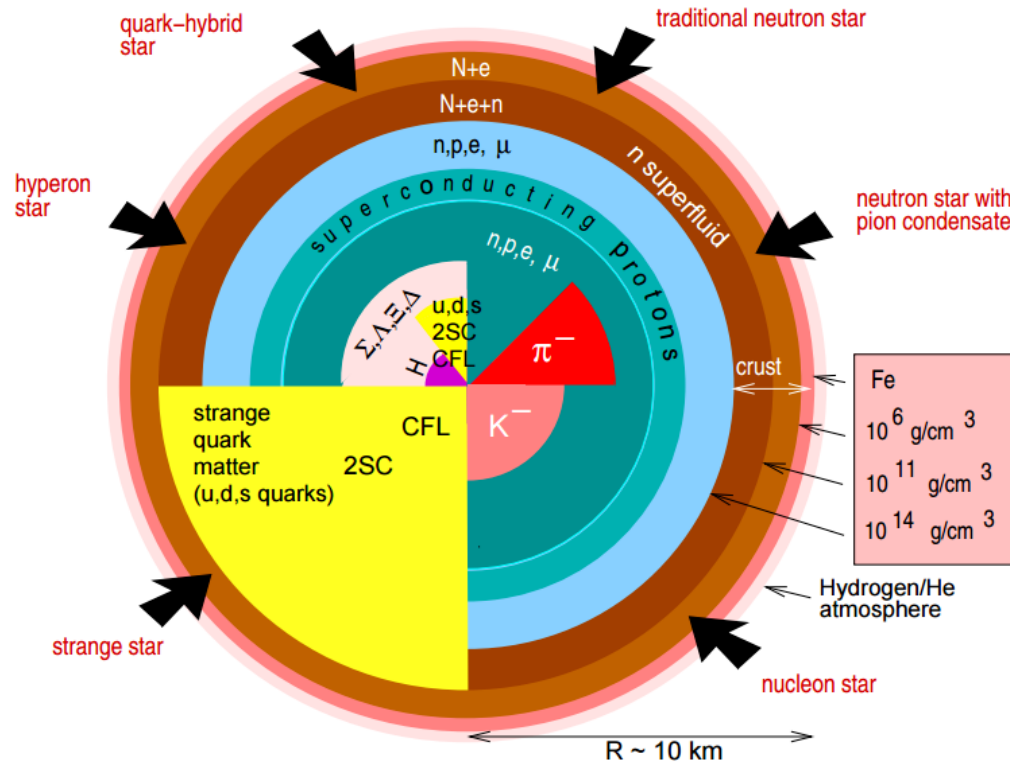




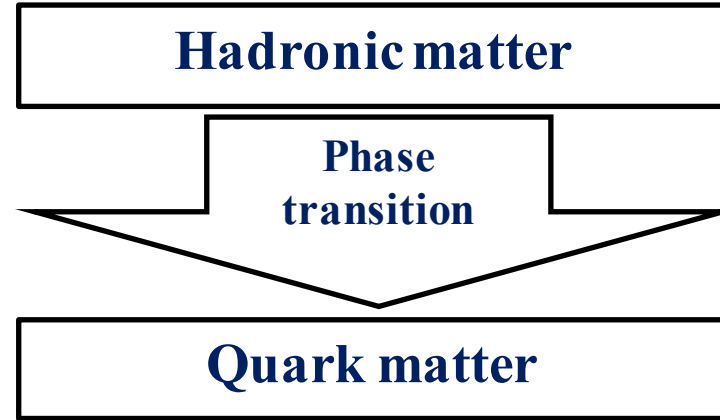
# Outline

- *Introduction*
- *Theoretical framework*
- *Numerical results*
- *Summary*

# Introduction



F. Weber, *Prog. Part. Nucl. Phys.* 54 (2005) 193-288.



PSR J1614-2230 [1,2]:  $1.928 \pm 0.017 M_{\odot}$   
 PSR J3048+0432 [3]:  $2.01 \pm 0.04 M_{\odot}$

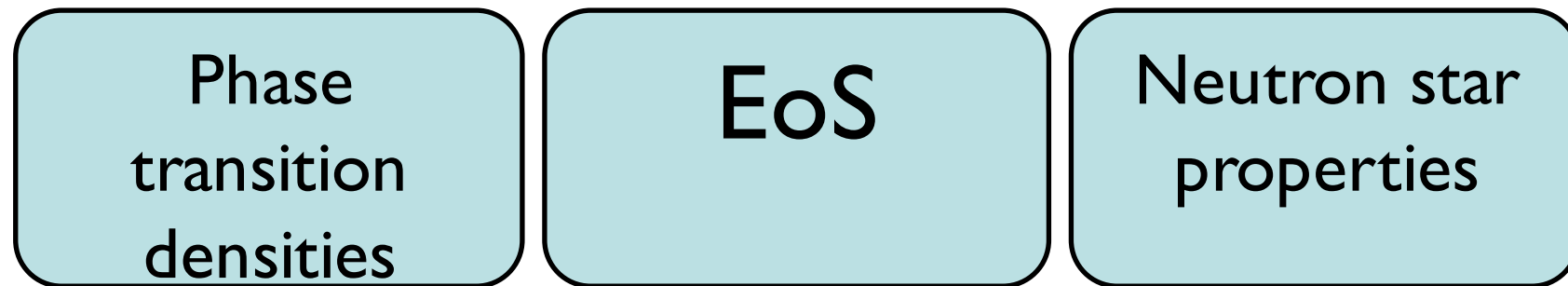
- [1] P. B. Demorest, T. Pennucci, S. M. Ransom, et al., *Nature* 467, 1081 (2010).
- [2] E. Fonseca, T. T. Pennucci, J. A. Ellis, I. H. Stairs, D. J. Nice, S. M. Ransom, P. B. Demorest, Z. Arzoumanian, K. Crowter, T. Dolch et al., *Astrophys. J.* 832, 167 (2016).
- [3] J. Antoniadis<sup>1</sup>, P. C. C. Freire<sup>1</sup>, N. Wex<sup>1</sup>, et al., *Science* 340, 6131 (2013).

# Introduction

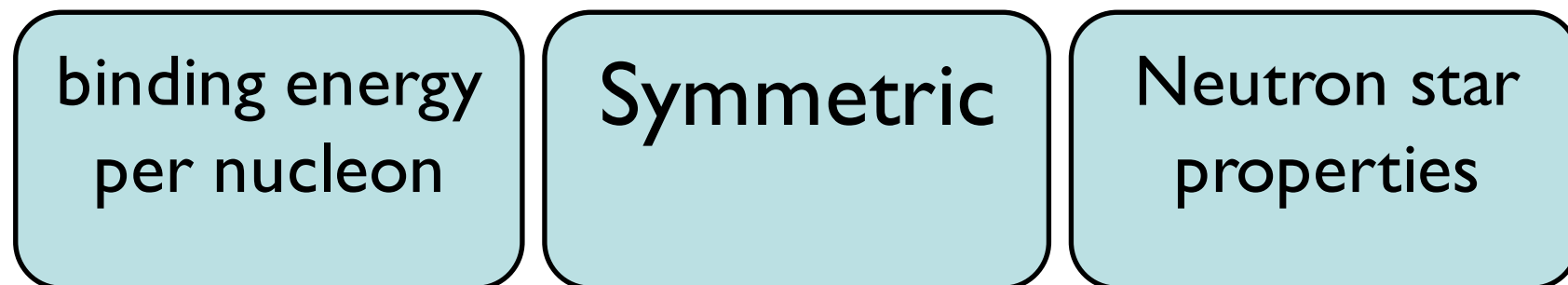


What do we want to know?

**Symmetry energy slope  $L$  dependence?**



**Isovector-vector coupling  $G_R$  dependence?**



# Theoretical framework



## Hadronic matter: (RMF)

$$\begin{aligned} \mathcal{L}_{\text{RMF}} = & \sum_{i=p,n} \bar{\psi}_i \left\{ i\gamma_\mu \partial^\mu - (M + g_\sigma \sigma) - \gamma_\mu \left[ g_\omega \omega^\mu + \frac{g_\rho}{2} \tau_a \rho^{a\mu} \right] \right\} \psi_i \\ & + \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 - \frac{1}{3} g_2 \sigma^3 - \frac{1}{4} g_3 \sigma^4 \\ & - \frac{1}{4} W_{\mu\nu} W^{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu + \frac{1}{4} c_3 (\omega_\mu \omega^\mu)^2 \\ & - \frac{1}{4} R_{\mu\nu}^a R^{a\mu\nu} + \frac{1}{2} m_\rho^2 \rho_\mu^a \rho^{a\mu} + \Lambda_V (g_\omega^2 \omega_\mu \omega^\mu) (g_\rho^2 \rho_\mu^a \rho^{a\mu}) \\ & + \sum_{l=e,\mu} \bar{\psi}_l (i\gamma_\mu \partial^\mu - m_l) \psi_l, \end{aligned}$$

## Quark matter:

### (NJL)

$$\begin{aligned} \mathcal{L}_{\text{NJL}} = & \bar{q} (i\gamma_\mu \partial^\mu - m^0) q + G_S \sum_{\alpha=0}^8 \left[ (\bar{q} \lambda_\alpha q)^2 + (\bar{q} i\gamma_5 \lambda_\alpha q)^2 \right] \\ & - K \left\{ \det [\bar{q} (1 + \gamma_5) q] + \det [\bar{q} (1 - \gamma_5) q] \right\} \\ & + \mathcal{L}_{\text{vector}} \\ \mathcal{L}_V = & -G_0 (\bar{q} \gamma^\mu q)^2 - G_3 \left[ (\bar{q} \gamma^\mu \lambda_3 q)^2 + (\bar{q} i\gamma^\mu \gamma_5 \lambda_3 q)^2 \right] \\ & - G_8 \left[ (\bar{q} \gamma^\mu \lambda_8 q)^2 + (\bar{q} i\gamma^\mu \gamma_5 \lambda_8 q)^2 \right] \end{aligned}$$

$$\mathcal{L}_{\text{vector}} = \begin{cases} 1. & -g_V (\bar{q} \gamma^\mu q)^2 \\ 2. & -G_V \sum_{\alpha=0}^8 \left[ (\bar{q} \gamma^\mu \lambda_\alpha q)^2 + (\bar{q} \gamma^\mu \gamma_5 \lambda_\alpha q)^2 \right] \\ & \text{MF} = -\frac{2}{3} G_V (\bar{q} \gamma^\mu q)^2 - G_V \sum_{\alpha=1}^8 \left[ (\bar{q} \gamma^\mu \gamma_5 \lambda_\alpha q)^2 \right] \\ 3. & -G_R \sum_{\alpha=1}^3 \left[ (\bar{q} \gamma^\mu \lambda_\alpha q)^2 + (\bar{q} \gamma^\mu \gamma_5 \lambda_\alpha q)^2 \right] \end{cases}$$

# Results



## Parameter set

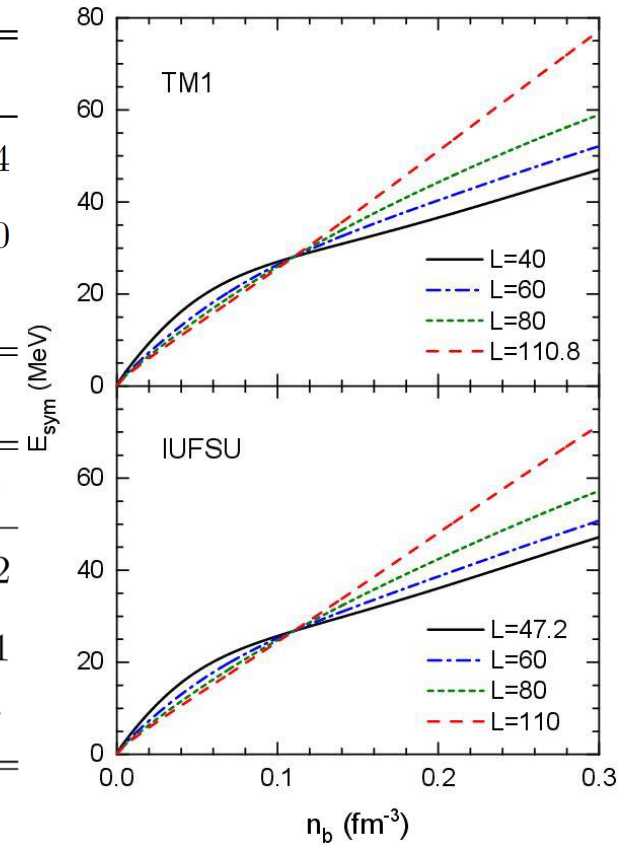
$$n_{\text{fix}} = 0.11 \text{ fm}^{-3}$$

### TM1 parameter set

$L$ (MeV)	40.0	50.0	60.0	70.0	80.0	90.0	100.0	110.8
$g_\rho$	13.9714	12.2413	11.2610	10.6142	10.1484	9.7933	9.5114	9.2644
$\Lambda_\nu$	0.0429	0.0327	0.0248	0.0182	0.0128	0.0080	0.0039	0.0000
$E_{\text{sym}}(n_0)$ (MeV)	31.38	32.39	33.29	34.11	34.86	35.56	36.22	36.89

### IUFSU parameter set

$L$ (MeV)	47.2	50.0	60.0	70.0	80.0	90.0	100.0	110.0
$g_\rho$	13.5900	12.8202	11.1893	10.3150	9.7537	9.3559	9.0558	8.8192
$\Lambda_\nu$	0.0460	0.0420	0.0305	0.0220	0.0153	0.0098	0.0051	0.0011
$E_{\text{sym}}(n_0)$ (MeV)	31.30	31.68	32.89	33.94	34.88	35.74	36.53	37.27



S. S. Bao, J. N. Hu, Z. W. Zhang, and H. Shen, Phys. Rev. C 90, 045802 (2014).

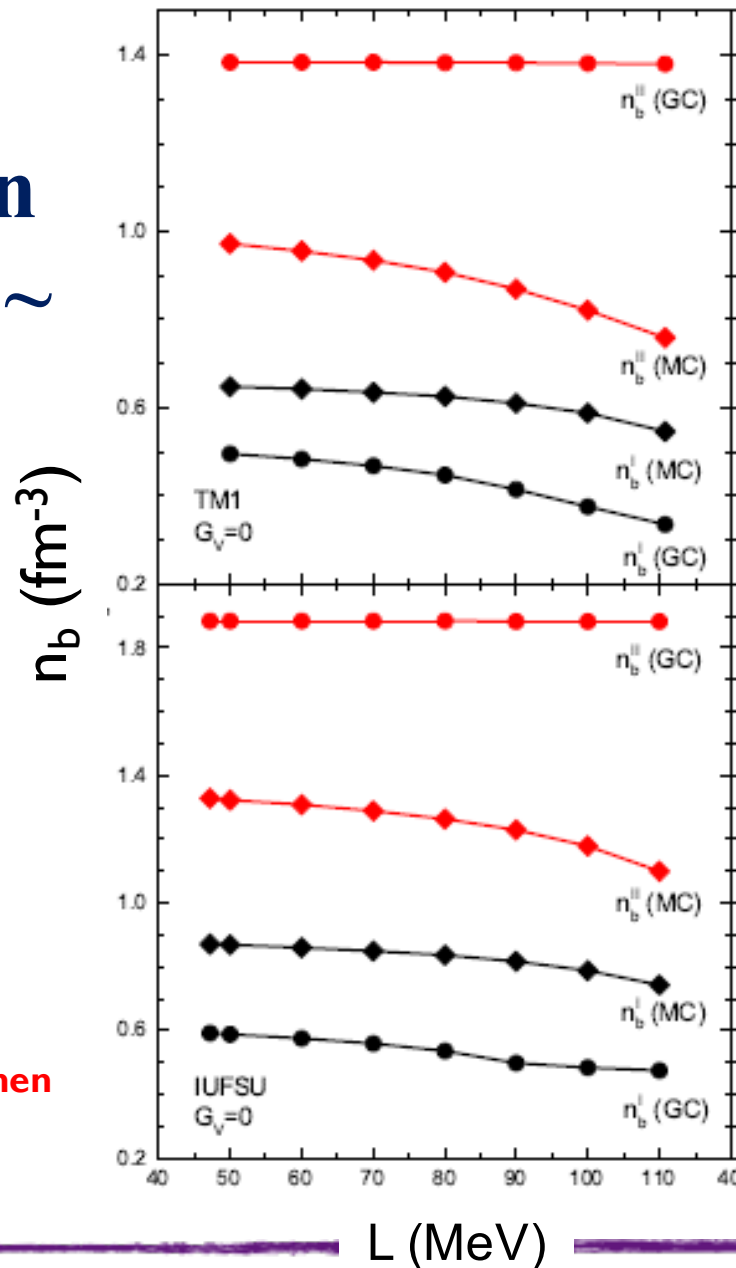
# Results (L dependence)



Phase transition densities  $\sim$  slope L

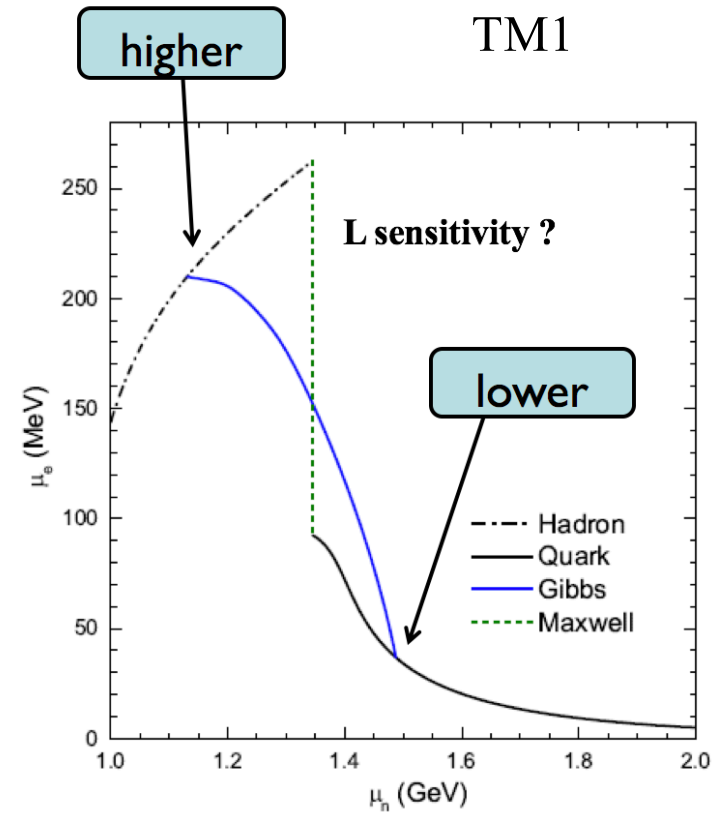
$n_b^i \searrow \sim L \nearrow$   
 $G_0 = 0$

X. H. Wu and H. Shen  
(in prep.)



$$\mu_e = \mu_n - \mu_p$$

$$\mu_e = \mu_d - \mu_u$$



# Results ( $L$ dependence)



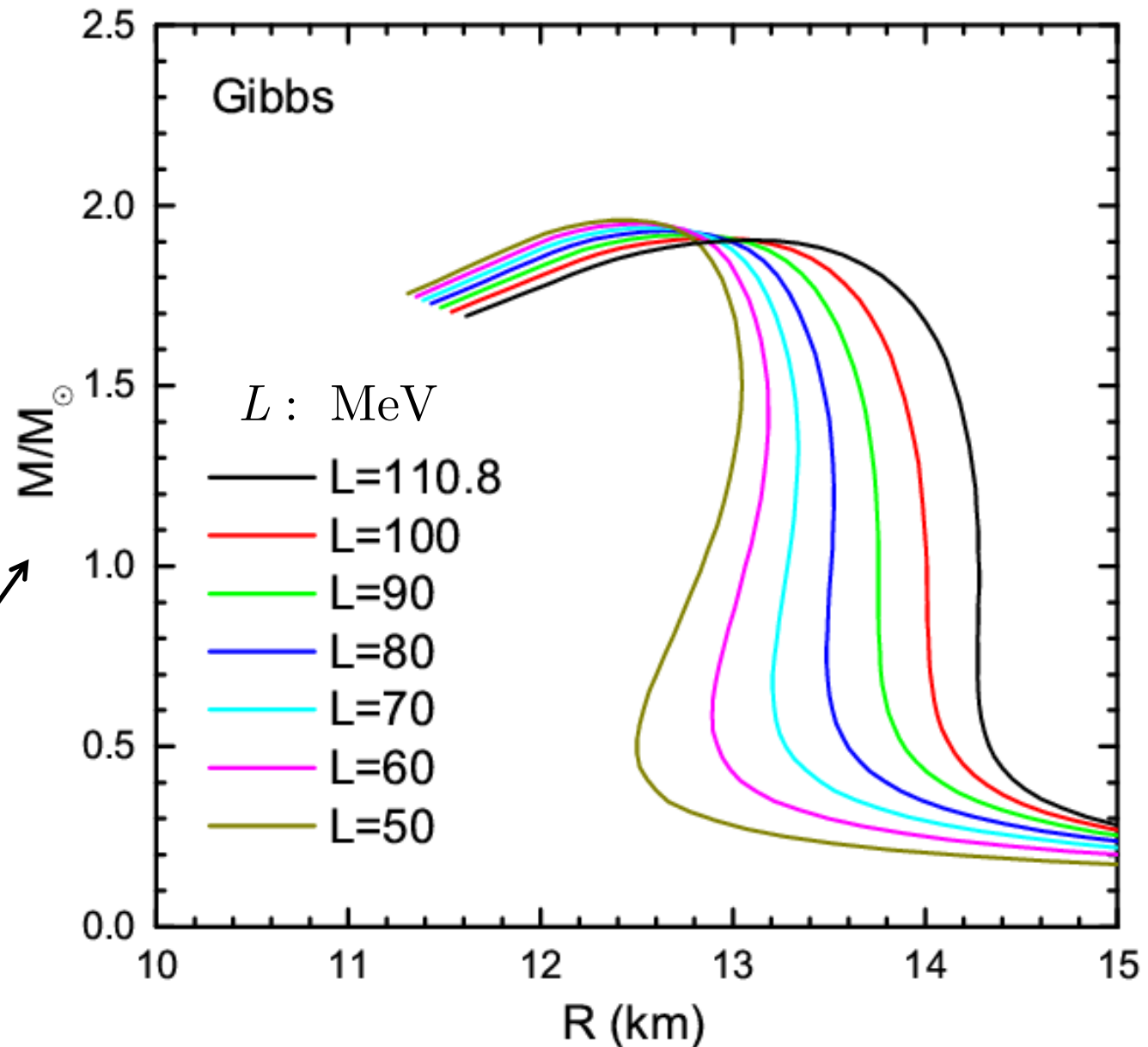
Mass-radius  
relations  
under Gibbs  
condition

$R \nearrow \sim L \nearrow$

TM1

$$G_0 = 0$$

X. H. Wu and H. Shen  
(in prep.)

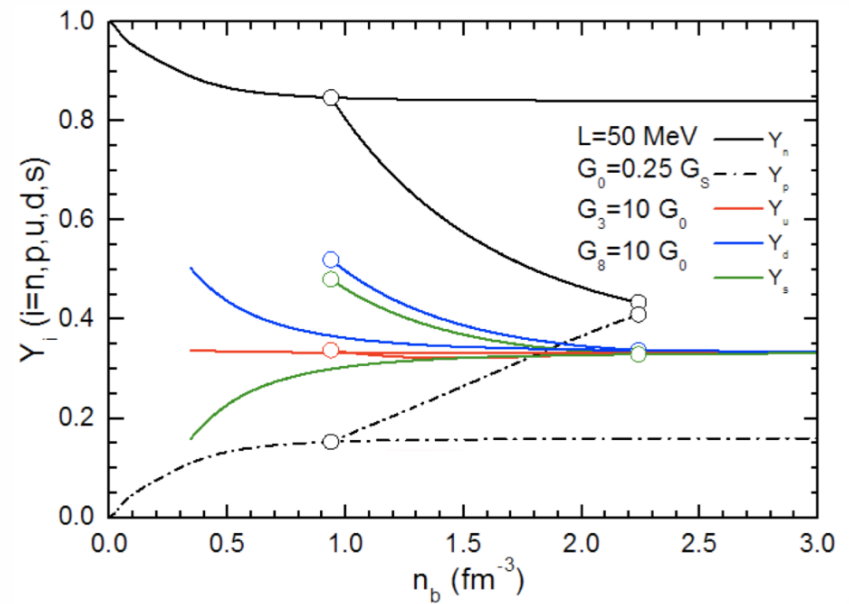
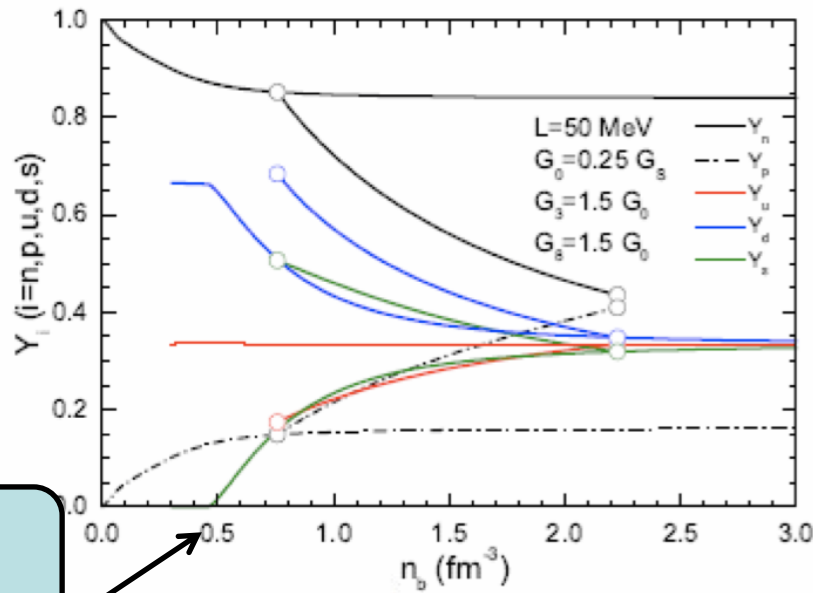
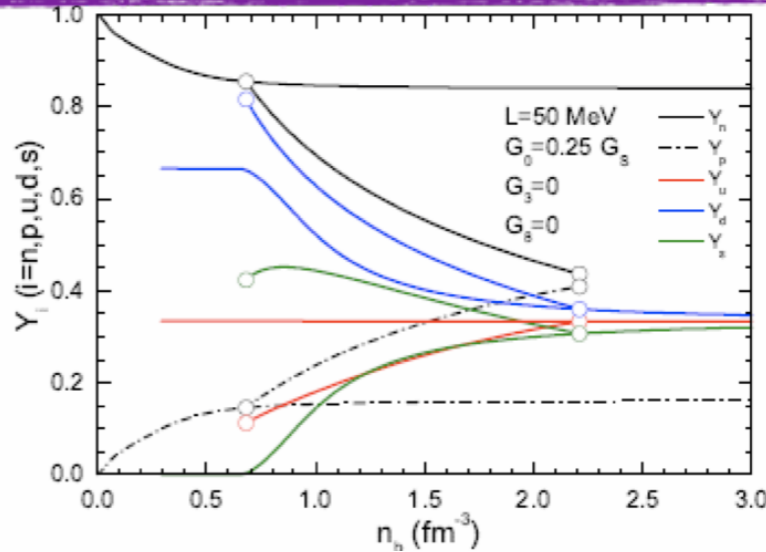




# Results (sym in QM)



## Particle number fraction



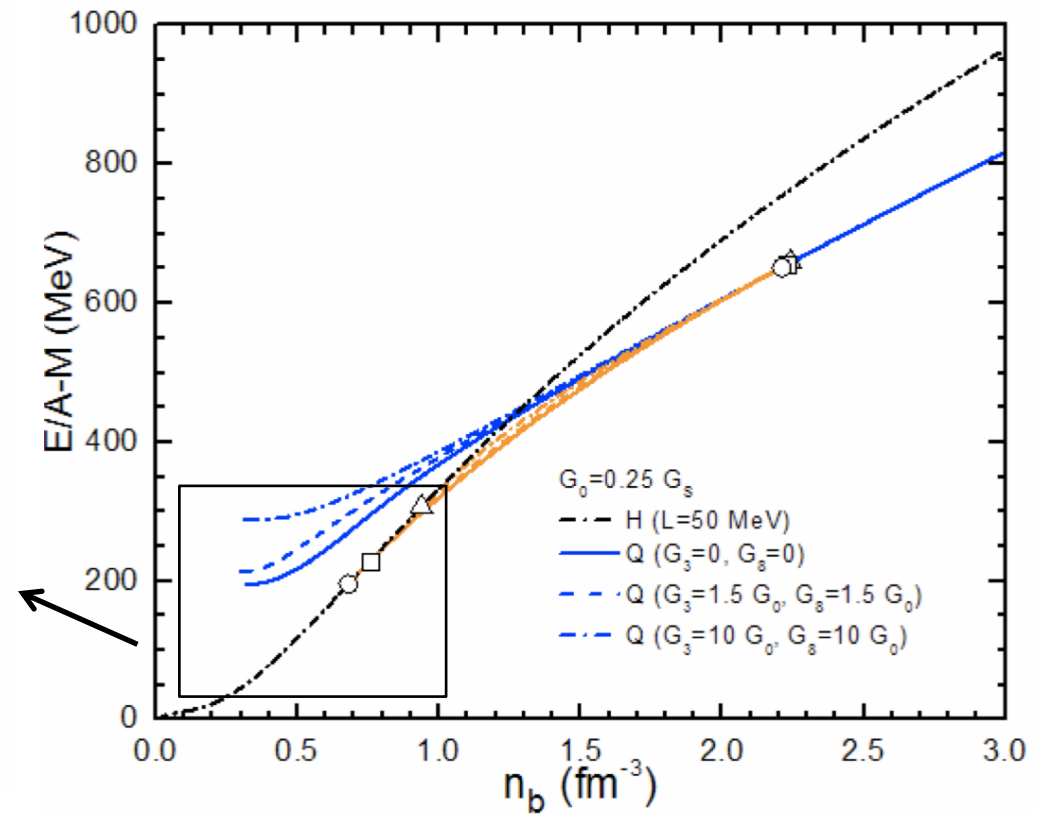
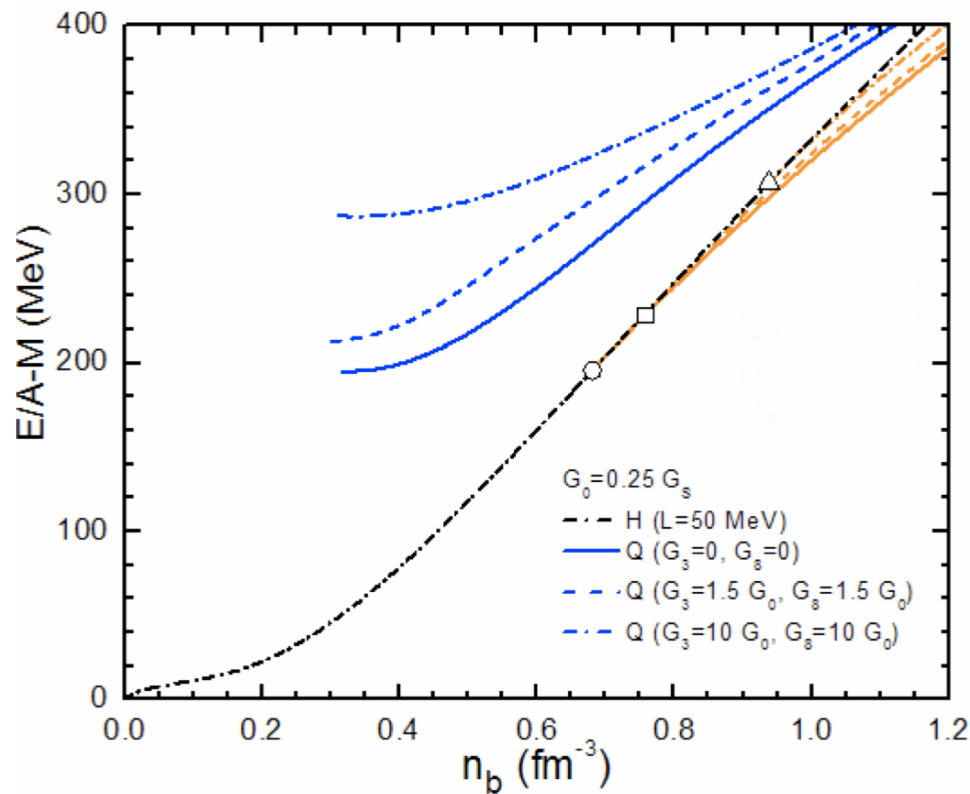
s quark appears

X. H. Wu, A. Ohnishi, H. Shen (in prep.)

# Results (sym in QM)



## Energy density per baryon



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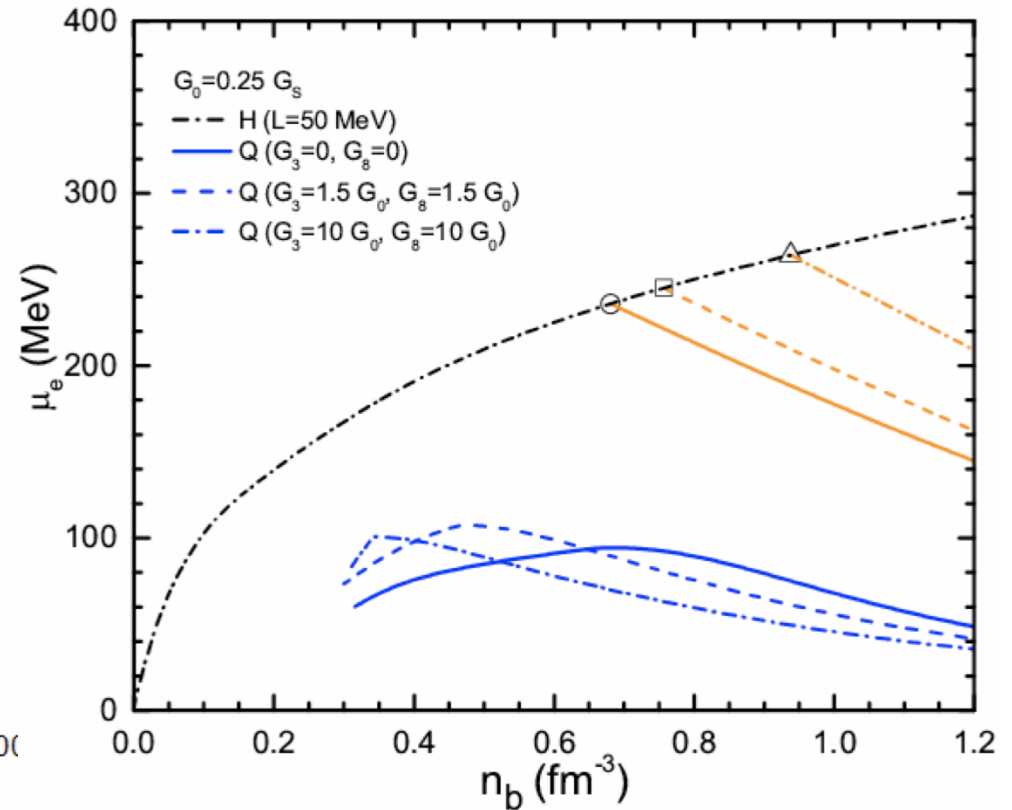
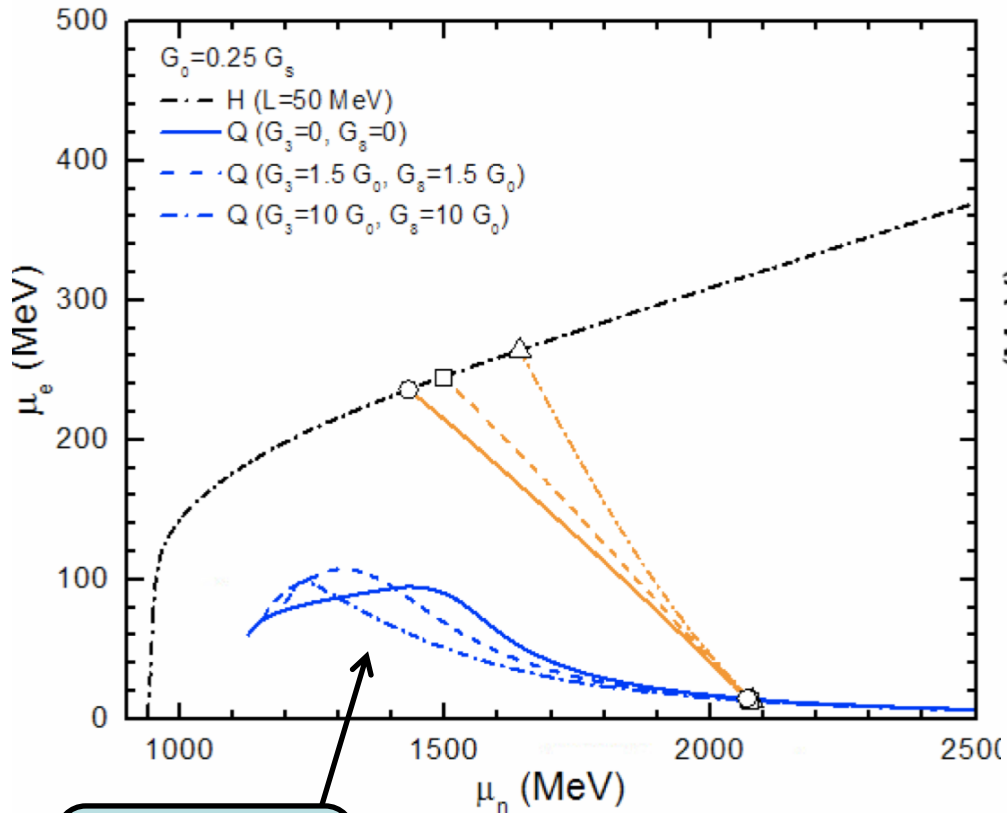
# Results (sym in QM)



## Electron chemical potential

$$\mu_e = \mu_n - \mu_p$$

$$\mu_e = \mu_d - \mu_u$$



s quark appears

X. H. Wu, A. Ohnishi, H. Shen (in prep.)

# Results (sym in QM)

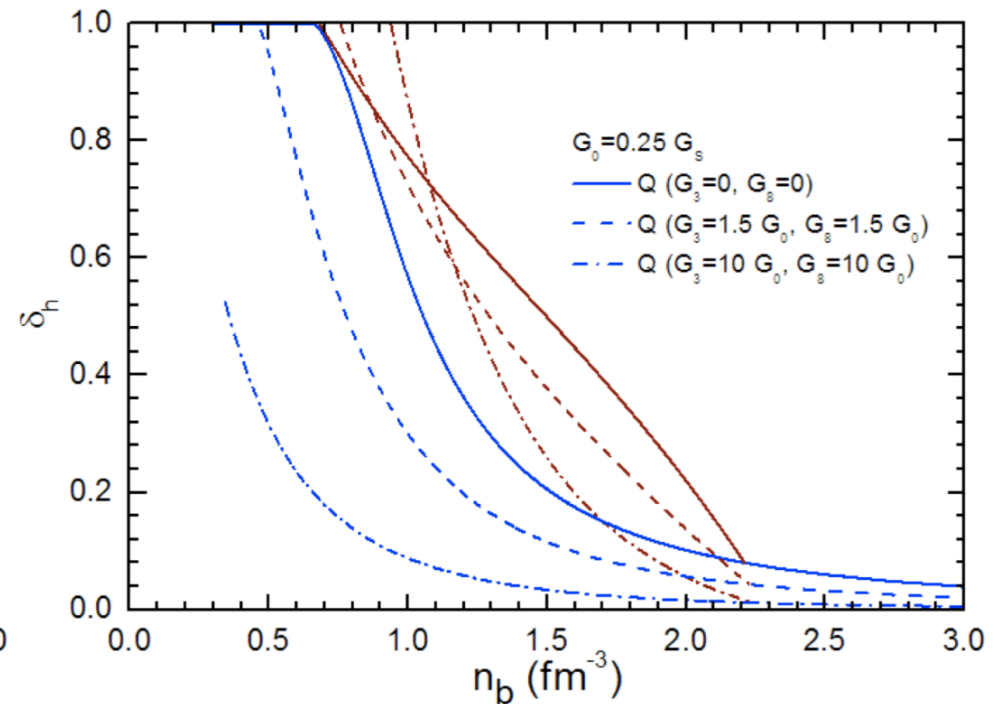
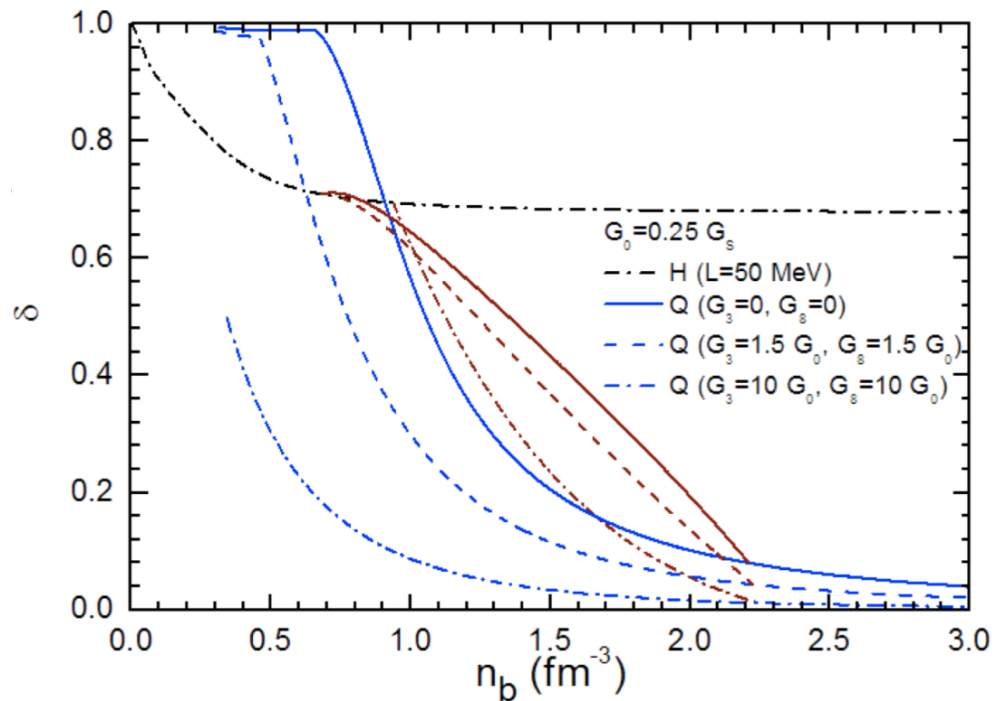


## Isospin asymmetry Hypercharge asymmetry

$$n_u = n_d = n_s$$



Charge  
neutrality



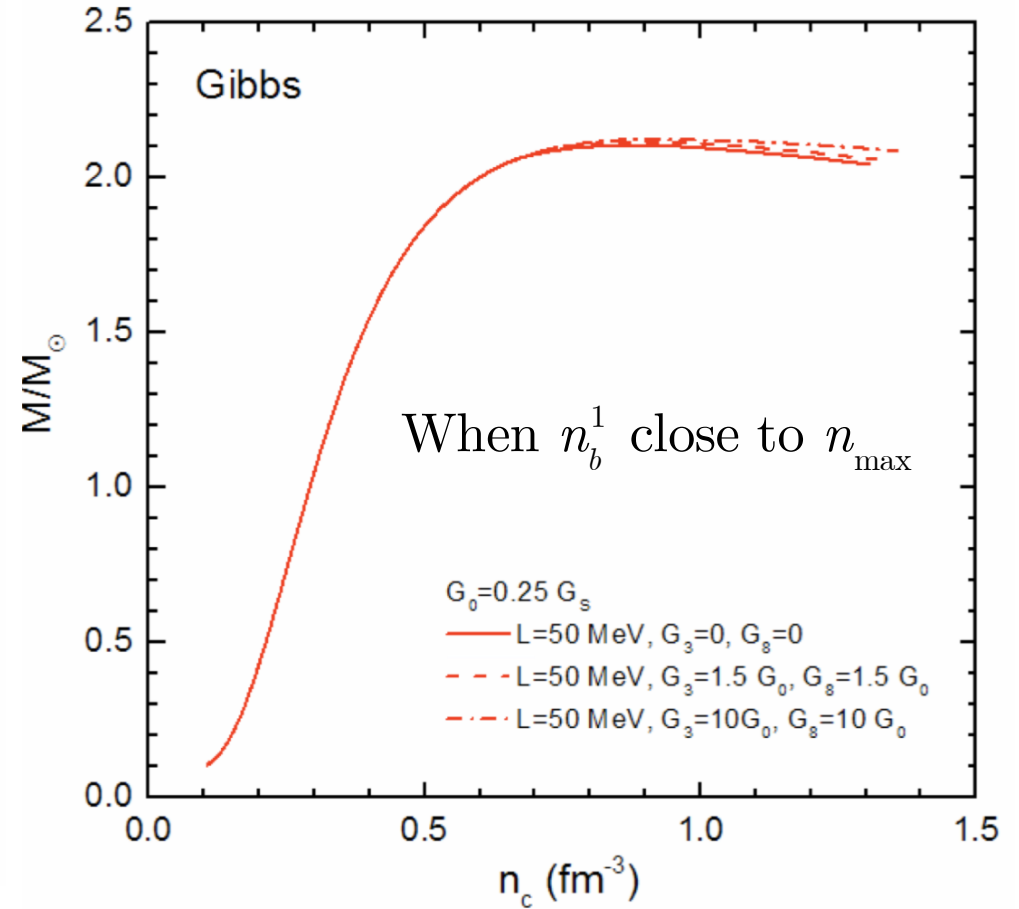
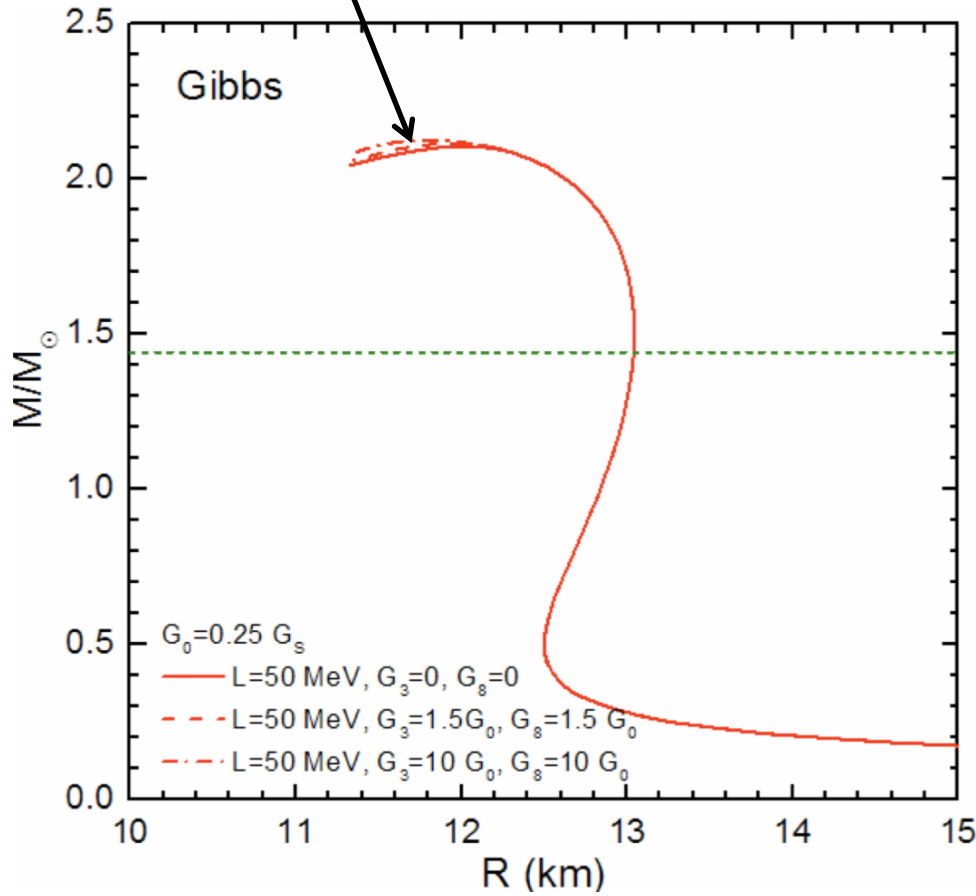
X. H. Wu, A. Ohnishi, H. Shen (in prep.)

# Results (sym in QM)



## Mass-radius relations

slighter increase



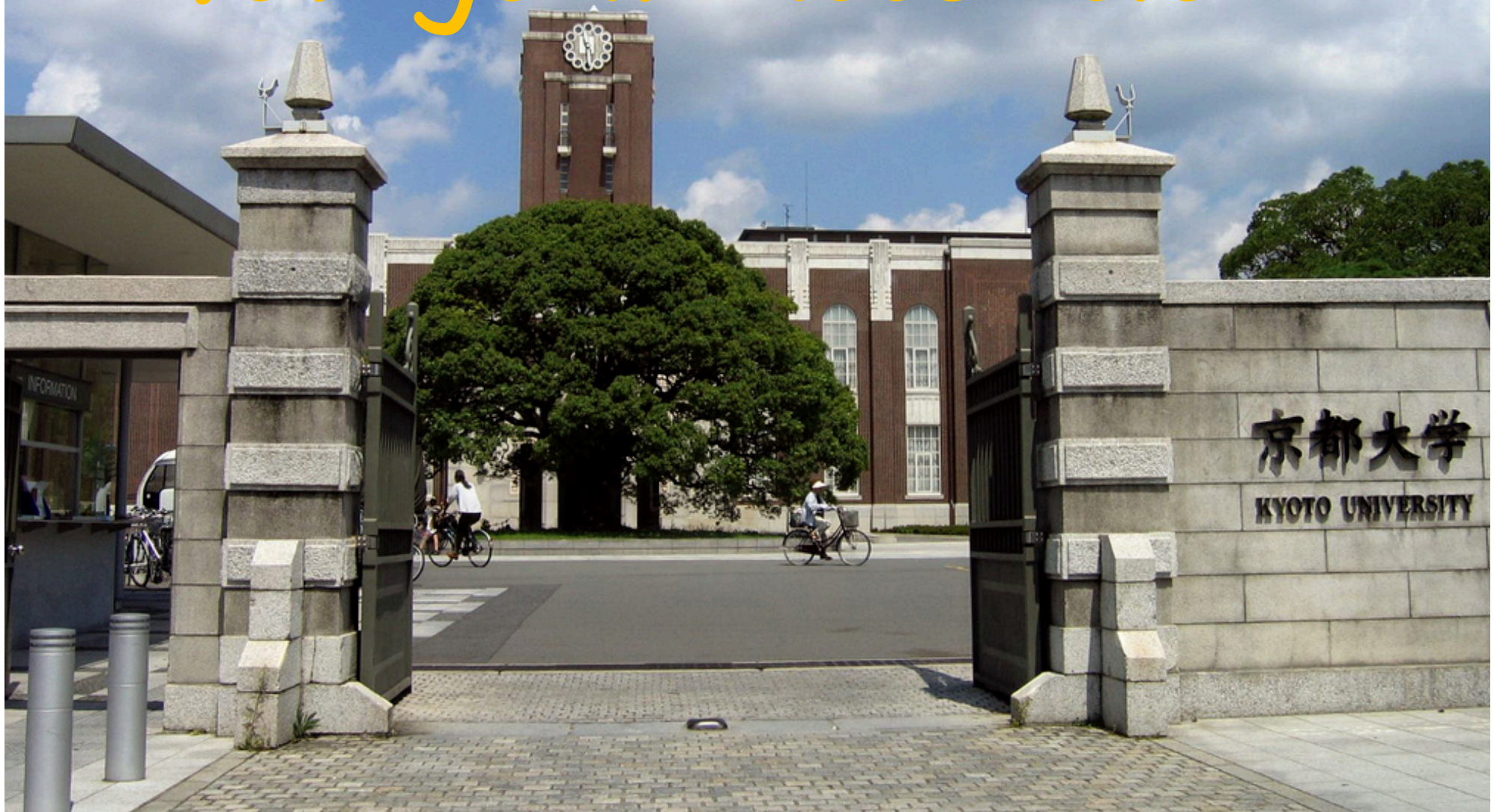
# Summary

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- 1. The hadron-quark phase transition densities decrease with slope  $L$  grow.**
  - 2. The isovector-vector coupling  $G_3$  and hypercharge coupling  $G_8$  in the NJL model can support higher neutron star mass.**
  - 3. The phase transition point close to the hadron phase are more sensitive to rho meson effect (slope  $L$  and couplings  $G_3$  ,  $G_8$ ).**
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*Thank you very much  
for your attention!*

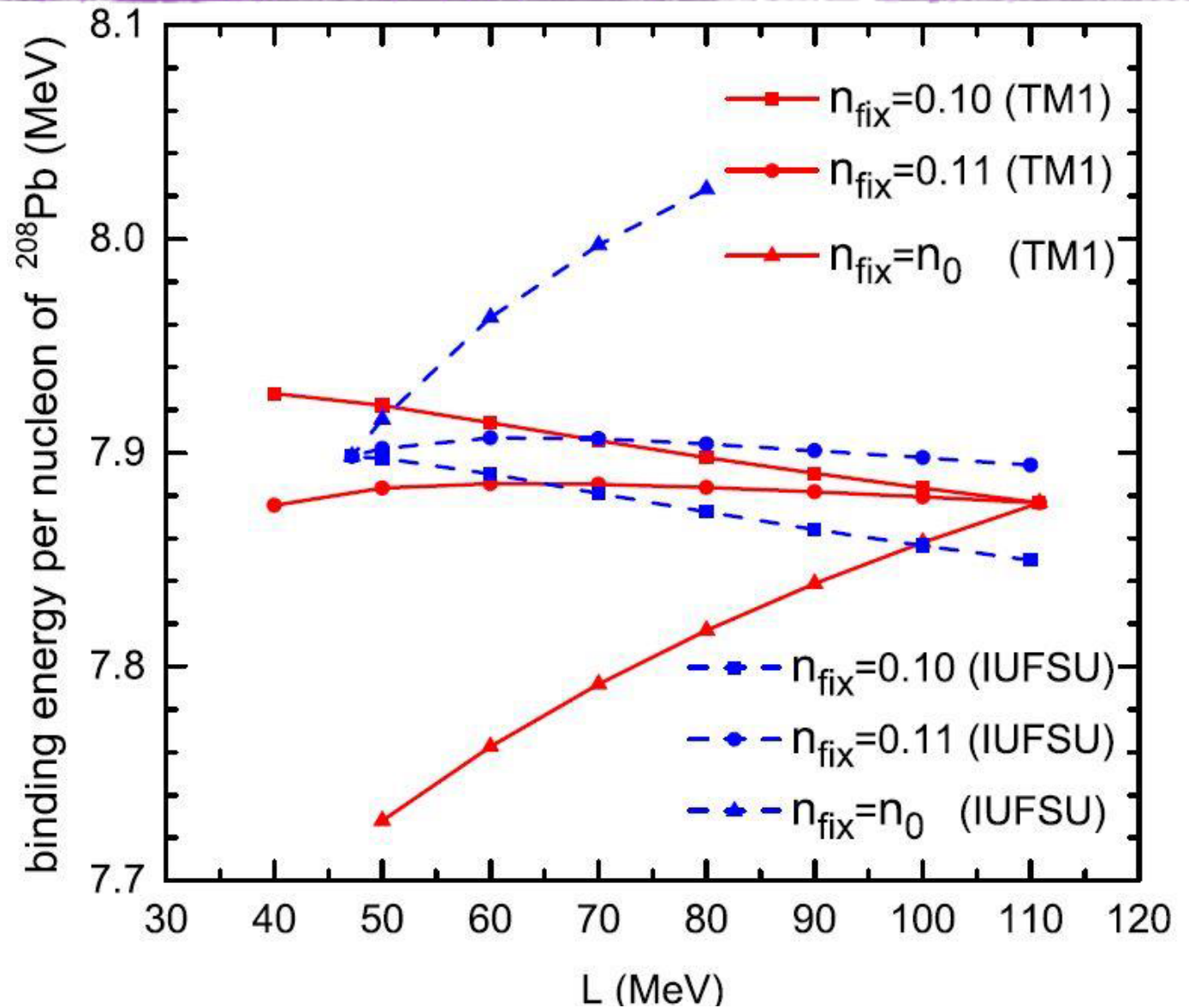


# Appendix



$$n_{\text{fix}} = 0.11 \text{ fm}^{-3}$$

Why ?



S. S. Bao, J. N. Hu, Z. W. Zhang, and H. Shen, Phys. Rev. C 90, 045802 (2014).