

Equations of State of Compact Star Matter with Clusters and Phase Transitions

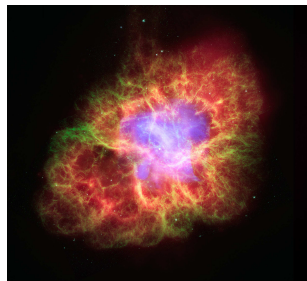
Stefan Typel



TECHNISCHE
UNIVERSITÄT
DARMSTADT

Workshop “Physics of Core-Collapse Supernovae and Compact Star Formations”

Waseda University, Tokyo, Japan
March 19 – 21, 2018



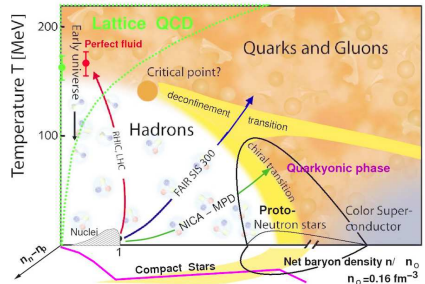
X-ray: NASA/CXC/J. Hester (ASU)
Optical: NASA/ESA/J. Hester & A. Loll (ASU)

- ▶ **Introduction**
- ▶ **Part 1:**
**Generalized Relativistic Density Functional
for Nuclei and Compact Star Matter**
- ▶ **Part 2:**
**CompStar Online Supernovae Equations of State
(CompOSE)**
- ▶ **Conclusions**

Introduction

development of a unified phenomenological description of

- ▶ **atomic nuclei**
 - ▶ light to (super-) heavy, stable and exotic
- ▶ **nuclear matter**
 - ▶ all relevant degrees of freedom
 - ▶ with phase transitions



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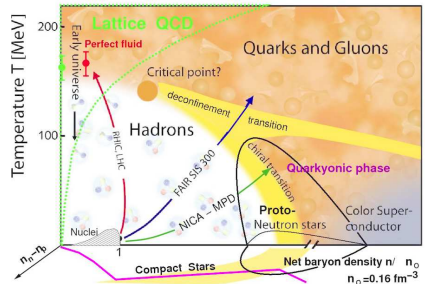
- ▶ light to (super-) heavy, stable and exotic

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- ▶ all relevant degrees of freedom
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▶ compact star matter

- ▶ for all densities, temperatures, and isospin asymmetries
- ▶ with inhomogeneities, clustering
- ▶ for neutron stars, their mergers and core-collapse supernovae



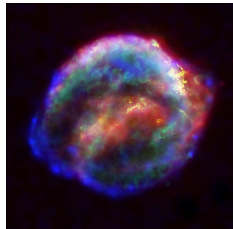
Equation of State (EoS) and Astrophysics I

essential ingredient in astrophysical model calculations

- ▶ static properties of **neutron stars**
- ▶ dynamical evolution of **core-collapse supernovae, neutron star mergers**
- ▶ conditions for **nucleosynthesis**
- ▶ energetics, **chemical composition**, transport properties



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NASA/ESA/R.Sankrit & W.Blair (Johns Hopkins Univ.)

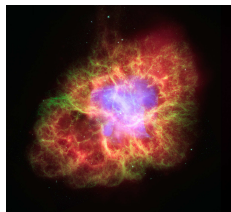
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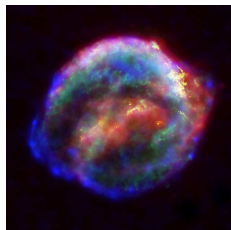
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timescale of reactions \ll timescale of system evolution

- ▶ **equilibrium** (thermal, chemical, ...)
- ▶ application of **EoS** reasonable



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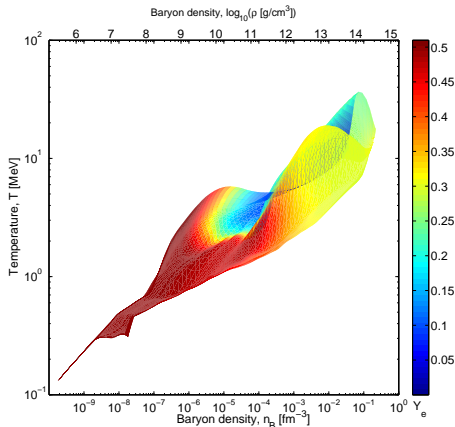
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Equation of State (EoS) and Astrophysics II

wide range of thermodynamic variables

- ▶ **temperature** T
- ▶ **baryon density** n_b
- ▶ **hadronic charge fraction** Y_q or
isospin asymmetry $\beta = 1 - 2Y_q$

simulation of core-collapse supernova



T. Fischer, Uniwersytet Wroclawski

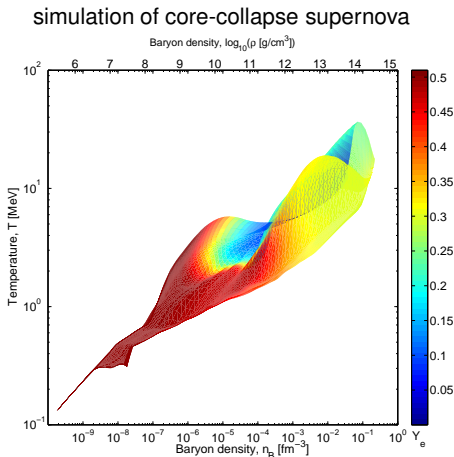
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modeling of nuclear matter
and stellar matter

- ▶ different systems and conditions



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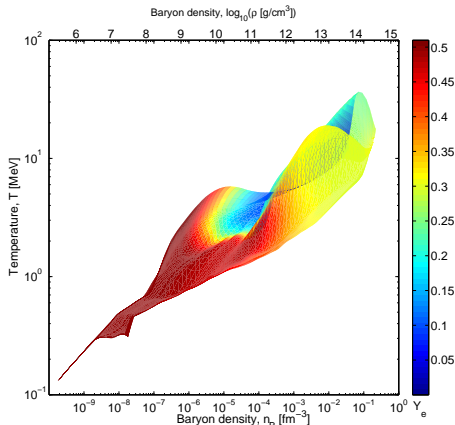
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- ▶ different systems and conditions

⇒ **global, multi-purpose EoS** required

EoS review: M. Oertel et al.,
Rev. Mod. Phys. 89 (2017) 015007

simulation of core-collapse supernova



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▶ hadronic 'ab-initio' methods with realistic interactions

- ▶ interactions: potential models, meson-exchange, chiral forces, RG evolved (Argonne, Urbana, Tucson-Melbourne, Nijmegen, Paris, Bonn, ...)
⇒ two-body NN interaction (in vacuum) well constrained by experiment, three-body forces less, large uncertainties for YN, YY, etc.
- ▶ many-body methods: BHF/DBHF, SCGF, CBF, VMC, GFMC, AFDMC, ...

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▶ QCD-based/inspired descriptions

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▶ effective field theories (EFT)

- ▶ chiral EFT, nuclear lattice EFT, ...

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- ▶ methods not always applicable (methodological/technical limitations)
- ▶ many EoS for neutron matter & neutron star matter, but no global EoS for astrophysical applications available from these approaches
⇒ only **phenomenological models** for global EoS at present



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- ▶ **global EoSs used in astrophysical simulations:**
 - ▶ H&W: W. Hillebrandt, K. Nomoto, R.G. Wolff, A&A 133 (1984) 175
 - ▶ LS180/220/375: J.M. Lattimer, F.D. Swesty, NPA 535 (1991) 331
 - ▶ STOS (TM1): H. Shen, H. Toki, K. Oyamatsu, K. Sumiyoshi, NPA 637 (1998) 435, PTP 100 (1998) 1013
 - ▶ HS (TM1,TMA,FSUgold,NL3,DD2,IUFSU): M. Hempel, J. Schaffner-Bielich, NPA 837 (2010) 210
 - ▶ SHT (NL3): G. Shen, C.J. Horowitz, S. Teige, PRC 82 (2010) 015806, 045802, PRC 83 (2011) 035802
 - ▶ SHO (FSU1.7, FSU2.1): G. Shen, C.J. Horowitz, E. O'Connor, PRC 83 (2011) 065808
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 - ▶ recently many more, also with additional degrees of freedom (hyperons, quarks)



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- ▶ **challenge:**
covering of full range of thermodynamic variables in a unified model
⇒ here: generalized relativistic density functional



Generalized Relativistic Density Functional for Nuclei and Compact Star Matter



- ▶ **objective:** development of improved EoS model with
 - ▶ extended set of constituent particles
 - ▶ *nuclear matter*: nucleons, nuclei/clusters, . . . , mesons, hyperons, . . . , quarks
 - ▶ *stellar matter*: add electrons, muons, photons



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 - ▶ correct treatment of phase transitions
 - ▶ distinguish nuclear matter and stellar matter
 - ▶ “non-congruent” phase transitions, gas/liquid/solid(crystal) phases



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only a selection from these topics considered here



basic approach: relativistic mean-field (RMF) models

- ▶ **energy density functional**
 - ▶ origin: field theoretical description
 - ▶ derived from Lagrangian density, mean-field approximation
 - ▶ phenomenological description



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- ▶ interaction: exchange of scalar and vector mesons ($\sigma, \omega, \rho, \dots$)
 - ▶ minimal coupling of mesons to nucleons
 - ▶ with nonlinear self-interactions
 - ▶ with density dependent couplings
- ▶ without explicit meson fields
 - ▶ point-coupling models



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▶ many parametrizations

- ▶ different purposes (finite nuclei, excitations, EoS, ...)

(see, e.g., M. Dutra et al., Phys. Rev. C 90 (2014) 055203)



► interaction contribution to Lagrangian

- nonlinear (NL) RMF models with meson self-interactions

$$\mathcal{L}_{\text{int}} = \bar{\psi} g_{\sigma} \sigma \psi - \frac{A}{3} \sigma^3 - \frac{B}{4} \sigma^4 - \bar{\psi} g_{\omega} \omega_{\mu} \gamma^{\mu} \psi + \frac{C}{4} (\omega_{\mu} \omega^{\mu})^2 - \bar{\psi} g_{\rho} \vec{\rho}_{\mu} \cdot \vec{\tau} \gamma^{\mu} \psi$$

with constants g_{σ} , g_{ω} , g_{ρ} , A , B , C , ...

(usually scalar and vector contributions not coupled, cross terms added later)



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- density dependent (DD) RMF models

$$\mathcal{L}_{\text{int}} = \bar{\psi} \Gamma_{\sigma} \sigma \psi - \bar{\psi} \Gamma_{\omega} \omega_{\mu} \gamma^{\mu} \psi - \bar{\psi} \Gamma_{\rho} \vec{\rho}_{\mu} \cdot \vec{\tau} \gamma^{\mu} \psi$$

with functionals Γ_{σ} , Γ_{ω} , Γ_{ρ} , ... depending on Lorentz scalars constructed from nucleon fields $\bar{\psi}$, ψ
(motivated by Dirac-Brueckner calculations, more flexible than NL models)

dependence of couplings Γ_i on

- vector density $\varrho^{(v)} = \sqrt{j^{\mu} j_{\mu}}$ with current $j^{\mu} = \bar{\psi} \gamma^{\mu} \psi \Rightarrow$ standard choice
- scalar density $\varrho^{(s)} = \bar{\psi} \psi \Rightarrow$ not really explored so far



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- **phenomenological approach** \Rightarrow model parameters determined from fits
(properties of finite nuclei, characteristic nuclear matter parameters)

Relativistic Density Functionals with Density Dependent Couplings

- ▶ first DD-RMF parametrization fitted to energies of selected nuclei:

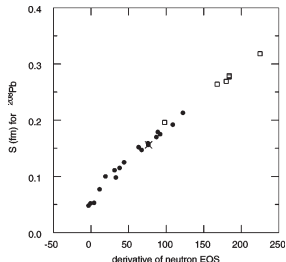
TW99 (S. Typel, H.H. Wolter, Nucl. Phys. A 656 (1999) 331)

- ▶ functional form of couplings: $\Gamma_i(\varrho) = \Gamma_i(\varrho_{\text{ref}})f_i(x)$
with $f_i(x) = a_j \frac{1+b_j(x+d_j)^2}{1+c_j(x+d_j)^2}$ or $f_i(x) = \exp[-a_j(x-1)]$ $x = \frac{\varrho}{\varrho_{\text{ref}}}$
- ▶ two parameters for isovector part of effective interaction (only one in standard NL-RMF models)
 - ⇒ improved nuclear matter parameters, similar to Skyrme Hartree-Fock models
 - ⇒ correlation of neutron skin thickness with slope of neutron matter EoS

	K [MeV]	J [MeV]	L [MeV]
TM1 [1]	285	36.9	110.8
NL3 [2]	272	37.4	118.5
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[1] Y. Sugahara and H. Toki, NPA 579 (1994) 557

[2] G.A. Lalazissis et al., PRC 55 (1997) 540



S. Typel and B.A. Brown, PRC 64 (2001) 027302

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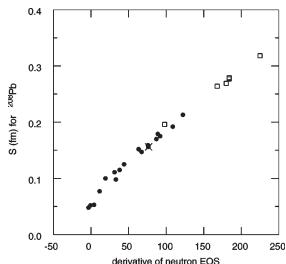
- ▶ many DD-RMF parametrizations in the following

- ▶ DD-ME1 (T. Nikšić et al., PRC 66 (2002) 024306)
- ▶ DDH δ (T. Gaitanos et al., NPA 732 (2004) 24)
- ▶ DD (S. Typel, PRC 71 (2005) 064301)
- ▶ DD-ME2 (G.A. Lalazissis et al., PRC 71 (2005) 024312)
- ▶ DD-F (T. Klähn et al., PRC 74 (2006) 035802)
- ▶ DD2 (S. Typel et al., PRC 81 (2010) 015803)
- ▶ DD-ME δ (X. Roca-Maza et al., PRC 84 (2011) 054309)
- ▶ DD+++ – DD $^{--}$ (S. Typel, PRC 89 (2014) 064321)
- ▶ ...

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► density dependence

- **'V'**: dependence of $\Gamma_\omega, \Gamma_\sigma, \Gamma_\rho$ on vector density $\varrho^{(v)}$
- **'S'**: dependence of $\Gamma_\omega, \Gamma_\sigma, \Gamma_\rho$ on scalar density $\varrho^{(s)}$
- **'M'**: dependence of $\Gamma_\omega, \Gamma_\rho$ (Γ_σ) on vector (scalar) density $\varrho^{(v)}$ ($\varrho^{(s)}$)



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► functional form for ω and σ mesons

- rational function $f_i(x) = a_i \frac{1+b_i(x+d_i)^2}{1+c_i(x+d_i)^2}$ with conditions $f_i(1) = 1$ and
- 'P': $f_i''(0) = 0, d_i > 0$ (positive)
- 'Z': $f_i'(0) = 0, d_i = 0$ (zero)
- 'N': $f_i''(0) = 0, d_i < 0$ (negative)



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► functional form for ρ meson

- 'E': exponential function $f_i(x) = \exp[-a_i(x-1)]$
- 'R': rational function $f_i(x) = a_i \frac{1+b_i(x+d_i)^2}{1+c_i(x+d_i)^2}$ with conditions
 $f_i(1) = 1, f_i'(0) = 0, d_i = 0, f_i''(1)/f_i(1) = f_i'''(1)/f_i'(1)$



▶ density dependence

- ▶ 'V': dependence of Γ_ω , Γ_σ , Γ_ρ on vector density $\varrho^{(v)}$
- ▶ 'S': dependence of Γ_ω , Γ_σ , Γ_ρ on scalar density $\varrho^{(s)}$
- ▶ 'M': dependence of Γ_ω , Γ_ρ (Γ_σ) on vector (scalar) density $\varrho^{(v)}$ ($\varrho^{(s)}$)

▶ functional form for ω and σ mesons

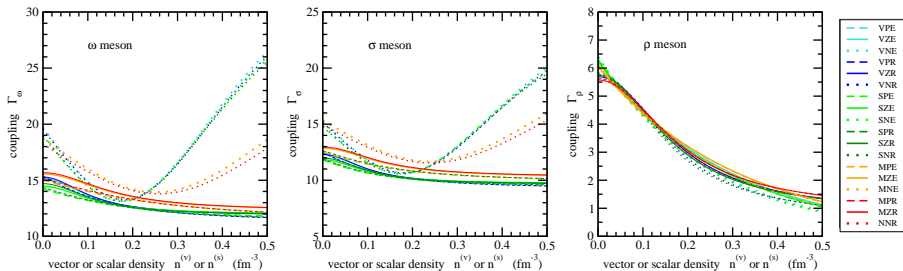
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 $f_i(1) = 1$, $f_i'(0) = 0$, $d_i = 0$, $f_i'(1)/f_i(1) = f_i''(1)/f_i'(1)$

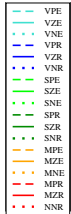
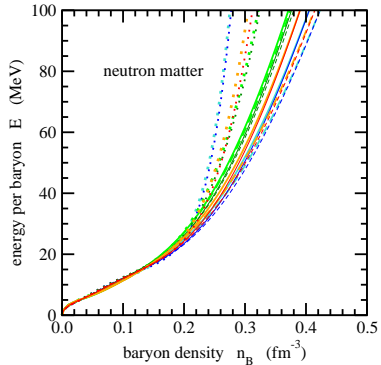
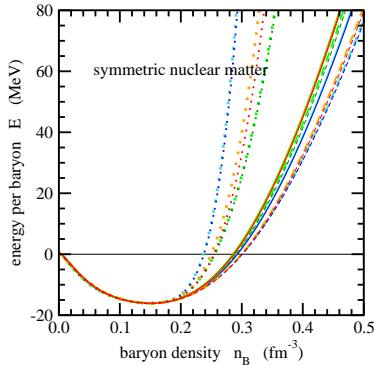
⇒ 18 models with 9 parameters (including ϱ_{ref} and m_σ),
fitted to properties of nuclei, similar quality in description,
details: S. Typel, Particles 1 (2018) 2

Coupling Functions



- ▶ similar smooth functions for 'P' and 'Z' parametrisations
- ▶ minimum in functions for 'N' parametrisations (ω and σ mesons)
- ▶ only small differences between 'E' and 'R' parametrisations (ρ meson)

Equations of State at Zero Temperature



- ▶ very similar below saturation density
- ▶ divergence above saturation density
- ▶ strong stiffening for 'N' parametrizations

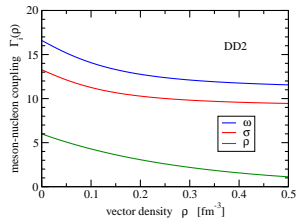
DD-RMF Parametrization DD2

► fitted to properties of finite nuclei

(S. Typel et al., PRC 81 (2010) 015803)

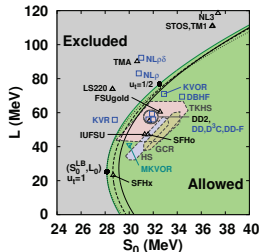
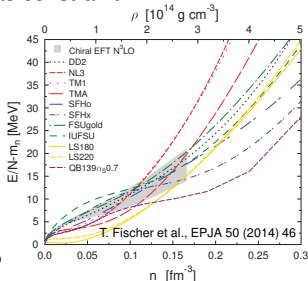
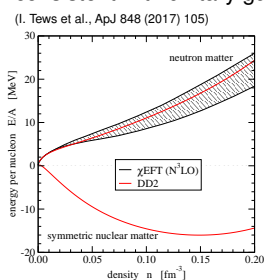
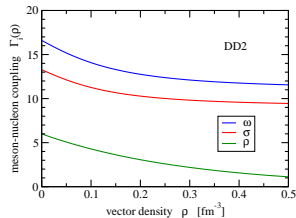
► very reasonable nuclear matter parameters

($n_{\text{sat}} = 0.149 \text{ fm}^{-3}$, $a_V = 16.02 \text{ MeV}$, $K = 242.7 \text{ MeV}$, $J = 31.67 \text{ MeV}$, $L = 55.04 \text{ MeV}$)



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- ▶ neutron matter EoS consistent with $\chi\text{EFT}(N^3\text{LO})$
(I. Tews et al., PRL 110 (2013) 032504, T. Krüger et al., PRC 88 (2013) 025802)
- ▶ consistent with unitary gas constraint
(I. Tews et al., ApJ 848 (2017) 105)





- ▶ **generalized relativistic density functional (gRDF)**
 - ▶ **extended set of particle species**
 - ▶ nucleons, electrons, muons, photons, hyperons (optional), . . .
 - ▶ light nuclei (${}^2\text{H}$, ${}^3\text{H}$, ${}^3\text{He}$, ${}^4\text{He}$) and heavy nuclei ($A > 4$)
 - ▶ AME2012/AME2016 mass tables (M. Wang et al., Chin. Phys. C 36 (2012) 1603; Chin. Phys. C 41 (2017) 030003)
 - ▶ extension with DZ10/DZ31 masses (J. Duflo and A.P. Zuker, Phys. Rev. C 52 (1995) R23)
- ⇒ shell effects included, full distribution, not only average heavy nucleus
- ▶ two-nucleon scattering states
- ⇒ consistency with virial EoS at low densities



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- ▶ **medium dependence of particle properties**
 - quasiparticle picture, mass shifts



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details: S. Typel et al., Phys. Rev. C 81 (2010) 015803; M. D. Voskresenskaya et al., Nucl. Phys. A 887 (2012) 42;
M. Hempel et al., Phys. Rev. C 91 (2015) 045805; S. Typel, arXiv:1504.01571; H. Pais et al., arXiv:1612.07022;
H. Pais et al. Nuovo Cim C 39 (2016) 393



- ▶ **concept applies to composite particles: clusters**
 - ▶ light and heavy nuclei
 - ▶ nucleon-nucleon correlations in continuum
- ▶ **effective change of binding energies**



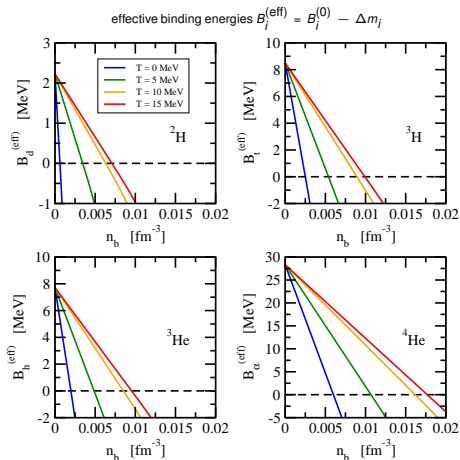
- ▶ **concept applies to composite particles: clusters**
 - ▶ light and heavy nuclei
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- ▶ **effective change of binding energies**
- ▶ **two major contributions** $\Delta m_i = \Delta m_i^{\text{strong}} + \Delta m_i^{\text{Coul}}$
 - ▶ strong shift $\Delta m_i^{\text{strong}}$
 - ▶ effects of strong interaction (coupling to mesons)
 - ▶ Pauli exclusion principle: blocking of states in the medium
 - ⇒ reduction of binding energies
 - ⇒ cluster dissolution at high densities: Mott effect
 - ⇒ replaces traditional excluded-volume mechanism
 - ▶ electromagnetic shift Δm_i^{Coul} (in stellar matter)
 - ▶ electron screening of Coulomb field
 - ⇒ increase of binding energies

▶ light nuclei

parametrization from G. Röpke,
simplified and modified for high
densities and temperatures

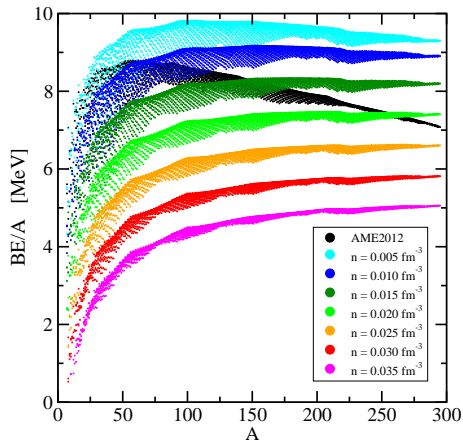
▶ NN scattering states

mass shifts as for deuteron



Mass Shifts III

- ▶ **light nuclei**
parametrization from G. Röpke,
simplified and modified for high
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- ▶ **NN scattering states**
mass shifts as for deuteron
- ▶ **heavy nuclei**
simple parametrization





emission of light nuclei

- ▶ determination of density and temperature of source
 - S. Kowalski et al. PRC 75 (2007) 014601
 - J. Natowitz et al. PRL 104 (2010) 202501
 - R. Wada et al. PRC 85 (2012) 064618
- ▶ thermodynamic conditions as in neutrinosphere of core-collapse supernovae



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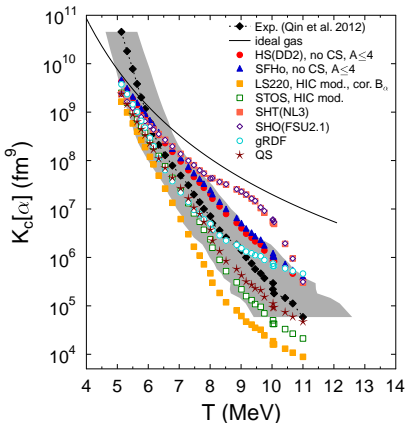
- ▶ thermodynamic conditions as in neutrinosphere of core-collapse supernovae

- ▶ particle yields \Rightarrow
chemical equilibrium constants

$$K_c[i] = n_i / (n_p^{Z_i} n_n^{N_i})$$

L. Qin et al., PRL 108 (2012) 172701

- ▶ mixture of ideal gases not sufficient



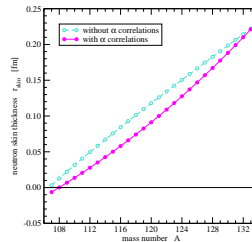
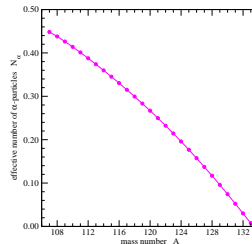
M. Hempel, K. Hagel, J. Natowitz, G. Röpke, S. Typel,
PRC C 91 (2015) 045805

Cluster Correlations at Nuclear Surface

▶ gRDF with clusters at zero temperature

- ▶ α -particles at surface of Sn nuclei
- ▶ reduced probability with increasing neutron excess
- ▶ reduction of neutron skin thickness

S. Typel, PRC 89 (2014) 064321



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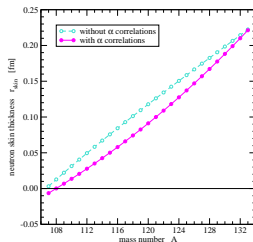
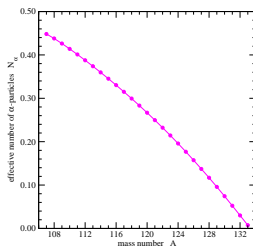
S. Typel, PRC 89 (2014) 064321

experimental tests

- ▶ quasifree (p,p α) **knockout** reactions, experiment with Sn nuclei in February 2018 at RCNP Osaka: successful detection of α particles with expected trend

- ▶ (d, ^6Li) **pickup** reactions
⇒ similar trend in reduced widths

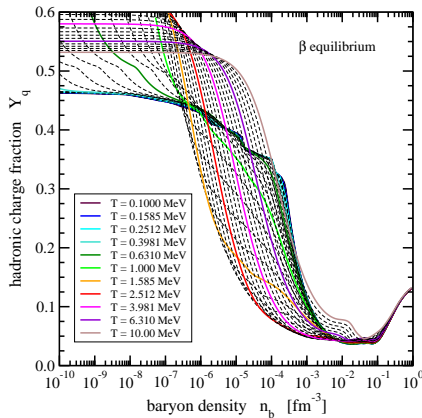
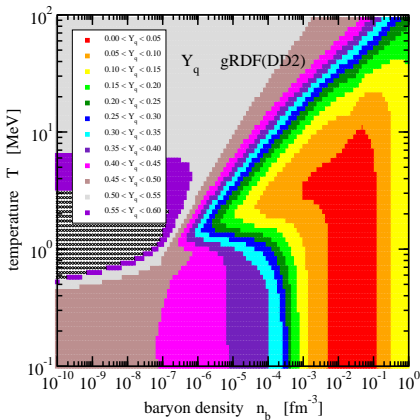
A. A. Cowley, Phys. Rev. C 93 (2016) 054329



Neutron Star Matter

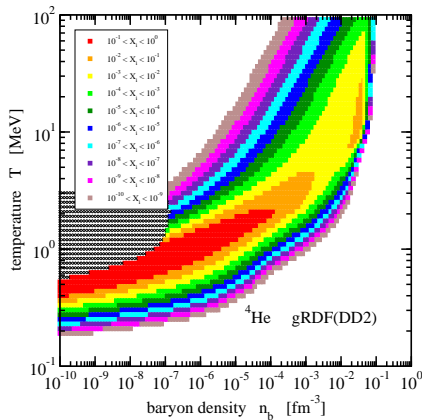
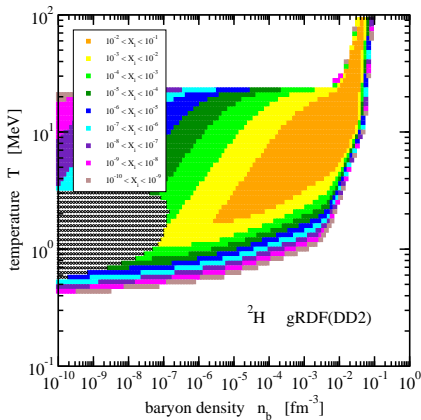
Hadronic Charge Fraction

► neutronization with increasing density

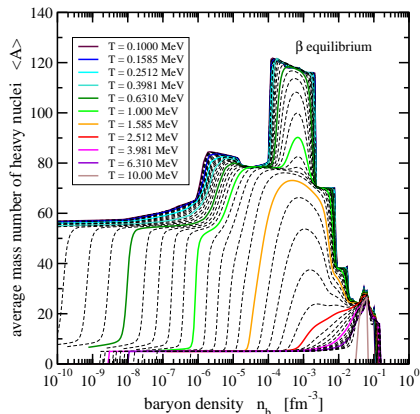
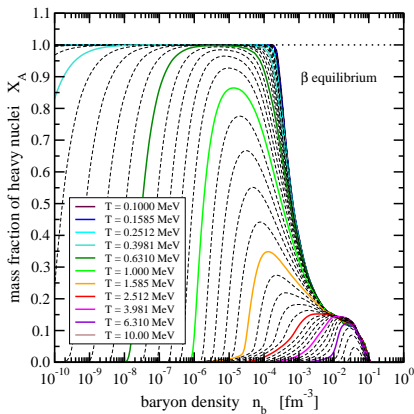


Neutron Star Matter Light Clusters

► mass fractions of ${}^2\text{H}$ and ${}^4\text{He}$



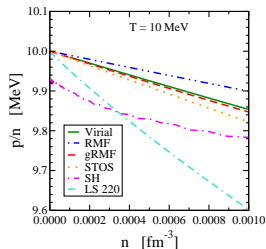
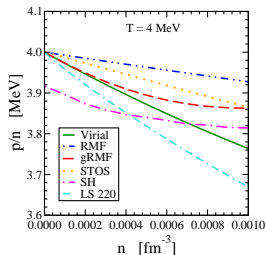
► mass fraction and average mass number



Low-Density Limit

- ▶ finite temperatures and very low densities: EoS determined by two-body correlations
- ▶ theoretical benchmark: **virial equation of state**
 - ▶ expansion of powers of fugacities
 - ▶ two-body correlations encoded in second virial coefficient
 - ▶ depends only on experimental data (phase shifts, binding energies)

(E. Beth and G. Uhlenbeck, Physica 3(1936) 729; Physica 4 (1937) 915,
C. J. Horowitz and A. Schwenk, NPA 776 (2006) 55)



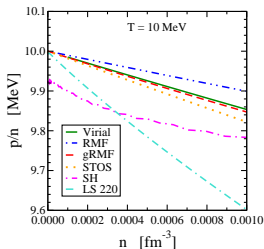
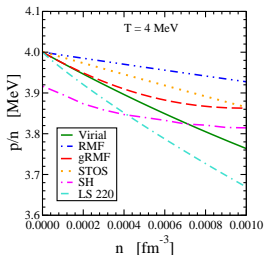
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C. J. Horowitz and A. Schwenk, NPA 776 (2006) 55)

- ▶ treatment in generalized relativistic density functional with two-body states as explicit degrees of freedom

(M. D. Voskresenskaya and S. Typel, NPA 887 (2012) 42)

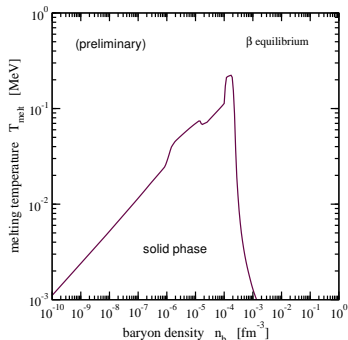


- ▶ **gap in EoS tables** between $T = 0$ and $T_{\min} > 0$
- ▶ **phase transition** from gas/liquid phase to solid phase
- ▶ correlations due to Coulomb interaction essential
- ▶ lattice-periodic Coulomb potential in crystal
- ▶ Wigner-Seitz approximation not sufficient

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- ▶ lattice-periodic Coulomb potential in crystal
- ▶ Wigner-Seitz approximation not sufficient
- ▶ better: effective Coulomb contribution from Monte Carlo simulation (molecular dynamics)
⇒ phase transition for **plasma parameter**

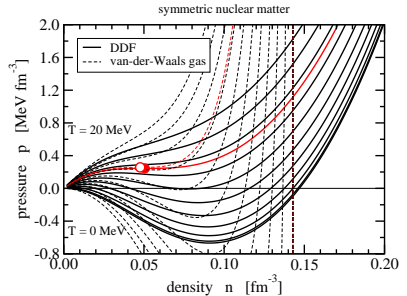
$$\Gamma = \frac{Z_{\text{ion}}^{5/3} e^2}{a_e T} \approx 175 \quad a_e = \left(\frac{3n_e}{4\pi} \right)^{1/3}$$

- ▶ improved description with model for crystal (in preparation)



example: symmetric nuclear matter

- ▶ isothermes in pressure-density diagram
⇒ **critical point**
 - ▶ DD-RMF:
 $T_c \approx 13.7 \text{ MeV}$,
 $n_c \approx 0.04515 \text{ fm}^{-3}$,
 $p_c \approx 0.180 \text{ MeV fm}^{-3}$
⇒ $p_c / (n_c T_c) \approx 0.290$
 - ▶ van-der-Waals gas:
⇒ $p_c / (n_c T_c) = 0.375$



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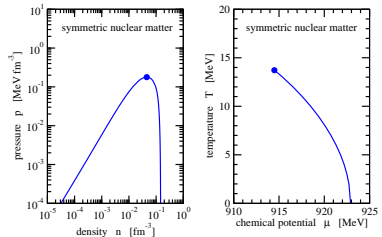
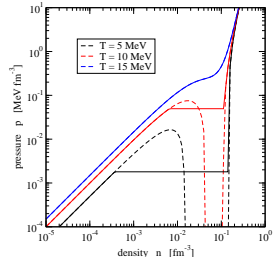
- ▶ DD-RMF:

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- ▶ van-der-Waals gas:
⇒ $p_c / (n_c T_c) = 0.375$

- ▶ $T < T_c$: **liquid-gas phase transition**

Maxwell construction
of coexisting phases
⇒ precursor of clustering





coexistence of phases

- ▶ general construction with Gibbs conditions:
equal intensive variables
 - ▶ temperature
 - ▶ pressure
 - ▶ chemical potentials

⇒ **binodals**
(enclose phase coexistence regions)

coexistence of phases

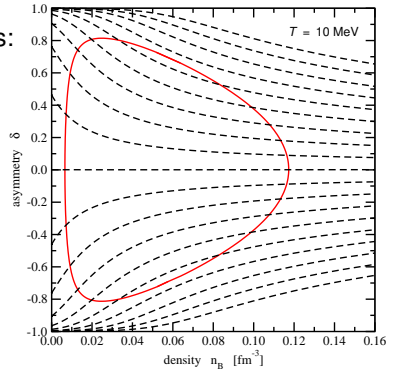
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▶ nuclear matter

- ▶ consider lines of equal charge chemical potential
 $\mu_q = \mu_p - \mu_n$
⇒ standard Maxwell construction
- ▶ symmetry with respect to isospin asymmetry



coexistence of phases

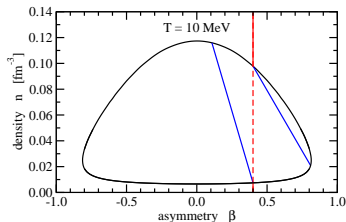
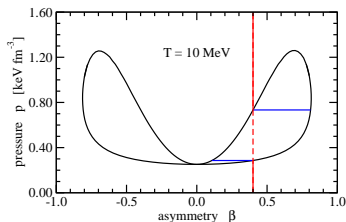
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coexistence of phases

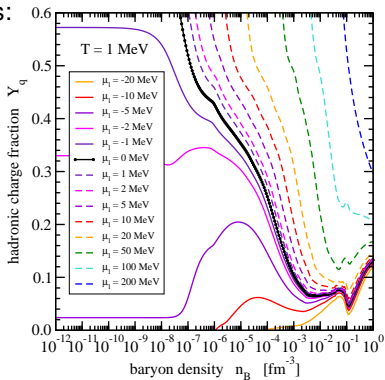
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⇒ **binodals**
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▶ supernova matter

- ▶ specific condition of charge neutrality
- ▶ consider lines of equal lepton chemical potential
 $\mu_l = \mu_e + \mu_q$
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- ▶ no symmetry with respect to isospin asymmetry



coexistence of phases

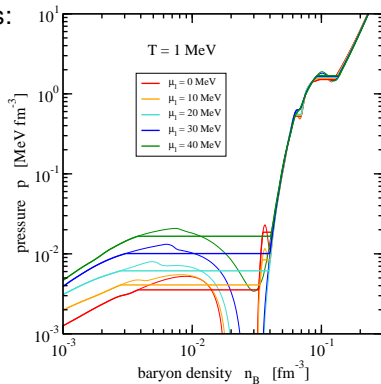
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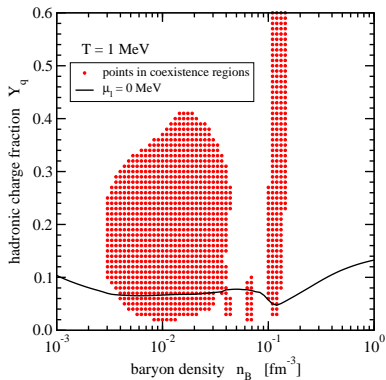
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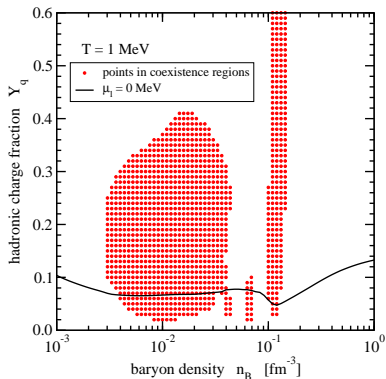
- ▶ full gRDF supernova EoS table with DD2 parametrization
 - ▶ baryon density: $10^{-12} \text{ fm}^{-3} \leq n_B \leq 1 \text{ fm}^{-3}$
 - ▶ temperature: $0.1 \text{ MeV} \leq T \leq 100 \text{ MeV}$
 - ▶ hadronic charge fraction: $0.01 \leq T_q \leq 0.60$



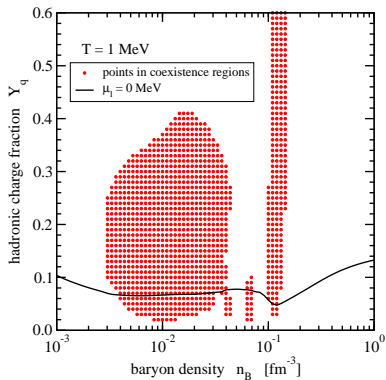
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⇒ **multiple phase transitions**

- ▶ coexistence of clustered and homogeneous phases
- ▶ coexistence of two clustered phases with different chemical composition



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- ▶ coexistence of clustered and homogeneous phases
 - ▶ coexistence of two clustered phases with different chemical composition
- ▶ global thermodynamic consistency of other EoS tables ?





CompStar Online Supernovae Equations of State (CompOSE)

CompOSE – Main Features



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- ▶ **free-access website (compose.obspm.fr)**
 - ▶ hosted at LUTH, Observatoire de Paris, Meudon



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- ▶ **repository of EoS tables**
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 - ▶ tabulation in temperature, baryon density and hadronic charge fraction
 - ▶ very flexible data format



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 - ▶ different output formats
- ▶ **documentation**
 - ▶ manual and 'how-to' instructions
 - ▶ bibliography of EoS publications
 - ▶ links to related projects



▶ core team

- ▶ Chikako Ishizuka (Tokyo Institute of Technology, Japan)
- ▶ Thomas Klähn (California State University Long Beach, USA)
- ▶ Micaela Oertel (LUTH, Observatoire de Paris, France)
- ▶ Stefan Typel (Technische Universität Darmstadt and GSI, Germany)

▶ web support

- ▶ Jean-Yves Giot (LUTH, Observatoire de Paris, France)
- ▶ Marco Mancini (LUTH, Observatoire de Paris, France)



- ▶ **presently available types of tables**
 - ▶ 3-dimensional
 - ▶ multi-purpose EoS (58 data sets)
 - ▶ 2-dimensional
 - ▶ zero-temperature EoS (5 data sets)
 - ▶ neutron matter EoS (26 data sets)
 - ▶ 1-dimensional
 - ▶ cold β -equilibrated matter EoS (27 data sets)

▶ presently available types of tables

- ▶ 3-dimensional
 - ▶ multi-purpose EoS (58 data sets)
- ▶ 2-dimensional
 - ▶ zero-temperature EoS (5 data sets)
 - ▶ neutron matter EoS (26 data sets)
- ▶ 1-dimensional
 - ▶ cold β -equilibrated matter EoS (27 data sets)

▶ EoS files

- ▶ parameters (temperature, baryon density and hadronic charge fraction):
`eos.t`, `eos.nb`, `eos.yq`
- ▶ EoS data: `eos.thermo`, `eos.compo*`, `eos.micro*` (*: optional)
- ▶ information on EoS model in data sheet: `eos.pdf`
- ▶ collection of files available as `eos.zip`

▶ software

- ▶ FORTRAN code, version 2.16
(`compose.f90`, `composemodules.f90`, `out_to_json.f90`, `Makefile`)
- ▶ old 'file version' (needs input files provided by the user)
- ▶ new 'terminal version' (default), simple interaction with user
- ▶ two output formats: ASCII and HDF5

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▶ output files

- ▶ EoS table: `eos.table`
- ▶ additional information: `eos.report`
- ▶ input for neutron star calculations (if possible): `eos.beta`



▶ web interface

- ▶ access restricted \Rightarrow registration required
- ▶ generation of EoS tables (in preparation)
- ▶ graphical representation of EoS etc.
(merger with EOSDB website in planning)



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▶ **LORENE library**

- ▶ cold neutron star EoS can be used as direct input for Nrotstar code
 \Rightarrow properties of rotating neutron stars



▶ manual

- ▶ detailed information on file formats, tabulation scheme, interpolation, . . .
- ▶ version 1.00 published (75 pages)
arXiv:1307.5715 [astro-ph.SR], Physics of Particles and Nuclei 46 (2015) 633
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▶ online bibliography

- ▶ links to original publications (61 entries)
- ▶ links to EoS data tables

▶ links to other EoS projects



▶ **submission of EoS data**

- ▶ contact CompOSE core team by sending email to `develop.compose@obspm.fr`
- ▶ details on preparation of files and transmission will be clarified

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▶ extension of EoS tables

- ▶ dependence on other variables?
(e.g. magnetic field strength, already implemented partly)
- ▶ choice of other primary variables?
- ▶ additional data (e.g. transport properties)?



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 - ▶ choice of other primary variables?
 - ▶ additional data (e.g. transport properties)?
- ▶ **different representation of data**
 - ▶ polynomials or other functions?
- ▶ **additional software**
 - ▶ conversion of tables?
- ▶ **extension of data base**
 - ▶ more EoS tables needed!
- ▶ **other suggestions?**

Conclusions



▶ EoS for simulations of Core-Collapse Supernovae

- ▶ big challenge for nuclear theory
- ▶ many aspects:
change of particle species, effective interaction, thermodynamics, . . .

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- ▶ **CompStar Online Supernovae Equations of State (CompOSE)**
 - ▶ repository of EoS tables
 - ▶ simple access
 - ▶ flexible data format
 - ▶ tools for data handling



Thank You